Equilibrium and kinetic studies of lead biosorption by three *Spirulina (Arthrospira)* species in open raceway ponds

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Abstract

The present investigation deals with the biosorption of lead from aqueous solutions in open race way pond using edible and live Spirulina (Arthospira) maxima, Spirulina (Arthospira) indica, Spirulina (Arthospira) platensis. Studies on various initial lead (II) ion concentrations, biosorbent dosage, pH and bioaccumulation potential were evaluated. The organisms are tolerant up to 4 mg/l and after that slight growth inhibition was found. Spirulina (Arthospira) indica showed more tolerance when compared with Spirulina (Arthospira) maxima and Spirulina (Arthospira) plantensis. The adsorption rate data was fitted to pseudo second order kinetics. The Langmuir and Freundlich models were applied to the experimental data and their equilibrium parameters were determined. Further optimization of initial lead (II) ion concentration, solution pH, agitation speed and biosorbent dosage were done using Box-Behnken experimental design coupled with artificial neural networks. This study provides a deep insight for exploring potential of using algal open race way ponds for biosorption of heavy metals. The diversity of the results can be expanded still further for other algal species and heavy metals.

Keywords: *Spirulina sp.*, Artificial Neural Networks (ANN), DIRECT algorithm, Box-Behnken design

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Introduction

Excessive use of heavy metals has seriously affected the environment and biodiversity of human, plant and animal population. Lead pollution has been considered as a major risk to air, soil and water. Batteries, pigment, plating, ammunition, rolled extrusions and cable sheathing are some industries responsible for release of lead in waste waters. Lead is a neurotoxic metal and its poisoning can cause severe mental or physical impairment. The recommended lead concentration by World Health Organization (WHO) in industrial waste streams is $10 \mu g/l$ (WHO 2011).

The recovery of lead from waste waters will become increasingly important to avoid further damage to the environment. Advanced techniques should be used with available resources for removal of lead from wastewaters before releasing to the water bodies. The use of microorganisms in the heavy metal removal has well documented since 19th century (Harris 1954; Dole 1952). Microorganisms, especially with their excellent surface properties and microscopic size are suitable targets for adsorption of heavy metal ions from solutions. The biological adsorption process has more advantages, when compared with conventional methods like chemical oxidation-reduction, precipitation, complexation, electrochemical operation, solidification, evaporation, adsorption, stabilization, vitrification, and ion exchange. The biosorption process can be highly selective, always provide with more surface area and easy adsorbent preparation, efficient and cost effective (Peters and Shem 1993; Puranik and Paknikar 1997; Puranik and Paknikar 1999).

The selective microorganism should always be safe for health and should be readily available. *Spirulina sp.* are multi-cellular and filamentous blue-green algae that had gained considerable popularity in the health and food industry. It is used as a protein and vitamin supplement to human, animal and aquaculture diets. It grows in Zarrouk's medium (Zarrouk et al. 1966) and can be harvested and processed easily and has a very high macro and micro-nutrient contents. Commercially, *Spirulina* alga is grown in outdoor raceway ponds in Earthrise farms, USA and Parry *Spirulina*, India. A raceway pond is an artificial pond with depth not more 4 feet and with varied length and breadth and can be used for the cultivation of algae in commercial scale. Presently, these open raceway ponds are also gaining popularity in algal biodiesel production (Rogers et al. 2014).

Biosorption using algae is considered to be easy when compared with other biosorption materials due to its availability and cost effectiveness. Chen and Pan (2004) studied the possibility of using live *Spirulina* to biologically remove aqueous lead below 50 mg/l from wastewater. Many studies on evaluating biosorption potential on pretreated or dead *Spirulina* biomass (Gong et al. 2005; Şeker et al. 2008; Solisio et al. 2006; Dotto et al. 2012; Babu et al. 2015; Markov et al. 2015; Kwak et al. 2015; Mitrogiannis et al. 2015; Deniz and Kepekci 2015) were available but very few biosorption studies were done on live *Spirulina sp* (Chen and Pan 2005; Hegde et al. 2015).

Statistical optimization techniques are powerful tools for handling complex data. Great quantities of experimental runs can often be reduced to more manageable proportions by performing of a few experiments which characterize the whole pattern of events and represents the entire set of combinations of factors. This can be achieved by applications of design of experiments. The experimental designs deal with the methods of analyzing variations in several factors simultaneously resulting in less number of experimental runs (Bailey Norman 1995). Box -Behnken experimental design can be easily applied to optimize variables when compared to factorial or fractional factorial designs. They require few experiments and effectively move through the experimental domain (Box and Behnken 1960). The results from the Box - Behnken experimental design were modeled using artificial neural networks and optimized using DIRECT (DIviding RECTangles) algorithm (Jones et al. 1993). Artificial neural networks (ANNs) are gaining importance due to the increase in the computational capacities and user friendly software technologies (Matlab, Mathworks, USA, Statistica, Statsoft, USA). The present work deals with the application of highly parallel computation based on distributed representation using Artificial Neural Networks (ANN) to solve and improvise the fitness of the data from the Box-Behnken experimental design and there by optimizing using DIRECT algorithm. These kind of advanced algorithms were rarely applied on complex biosorption data involving the adsorption of lead (II) ions using edible and live Spirulina (Arthospira) maxima, Spirulina (Arthospira) indica, and Spirulina (Arthospira) platensis in open raceway ponds.

Materials and Methods

Microorganism and media composition

Spirulina (Arthospira) maxima, Spirulina (Arthospira) indica, Spirulina (Arthospira) platensis were procured from Center for Advanced Studies, University of Madras, Chennai, Tamil Nadu, India and OfERR, Chennai. The organisms was first filtered and concentrated to 0.1 g/l and then inoculated in Zarrouk's medium (Table 1) and maintained for 7 days at 20~26°C under light generated by a 40 W white fluorescent lamp (Siva Kiran et al. 2012). The media components were added every 7 days to the culture flasks and water was replaced every 30 days for alga seed maintenance. Every two days, the alga seeds were monitored in the microscope for any contamination. pH of the solution was adjusted using sodium hydroxide and sulfuric acid. All chemicals used in study were procured from Merck, Germany (AR Grade) and the conductivity of the distillated water for chemicals preparation is 0.5 µmhos/cm.

Culture conditions

The Spirulina (Arthospira) maxima, Spirulina (Arthospira) indica, Spirulina (Arthospira) platensis growth characteristics were monitored by finding the optical density at 560 nm wavelength using UV-visible spectrophotometer (Shimadzu, Japan) at regular intervals. The biomass weight in grams was found by filtering *Spirulina (Arthospira)* species through Whatman No. 2 (8 μ m) filter paper and dried at 80°C for 4 h to 5 h until the sample reaches constant weight. The dry weight of the cell was determined after drying. Experiments were carried out in an open raceways pond (0.5 m long, 0.3 m wide, 0.075 m height) containing 3 l of *Spirulina (Arthospira)* cultures with an

Table 1: Composition of Zarrouk's Medium (Chen and Pan 2005)

Constituents	Concentration (g/L)
EDTA	0.08
CaCl ₂ .2H ₂ 0	0.04
NaCl	1.00
NaNO ₃	2.50
NaHCO ₃	16.80
FeSO ₄ .7H ₂ O	0.01
MgSO ₄ .7H ₂ O	0.20
K_2SO_4	1.00
K_2HPO_4	0.50

initial biomass concentration of 0.1 gdw/l. The cultures were illuminated with daylight-type 60 W fluorescent lights (Philips, India) at an intensity of 2000 lux in a 12 h light/dark photoperiod at $30^{\circ}C\pm 2^{\circ}C$. Lethal Concentration and time (LCt50) of lead (II) ion (Siva Kiran et al. 2012) were also calculated. Open raceway pond containing 3 L Zarrouk's medium with different concentrations of lead (II) ions (0, 1, 2, 4, 10 and 20 mg/l) and three *S. (Arthrospira)* culture (0.1 gdw/l) at 1:10 ratio were used for the growth and acute toxicity study and initial solution pH was measured to be 9. The growth rate was determined every 24 h for eight days in pond at each concentration and for each species (Siva Kiran et al. 2012).

Biosorption experiments

Lead solutions of the required concentrations were prepared by dissolving the exact quantities of PbNO₃, respectively, in distilled water. About 25 l of lead (II) solution was prepared by diluting standard PbNO3 solution to the desired concentrations. The biosorption experiments were conducted in another open raceway pond (0.7 m long * 0.3 m wide and 0.25 m height) with 25 l of freshly prepared lead solutions, with initial concentration 1 mg/l for 24 hours and biosorbant 0.24 g/l of Spirulina (Arthospira) maxima. Separate set of experiments with the same conditions were done by changing the organism to Spirulina (Arthospira) indica and Spirulina (Arthospira) platensis. Experiments were carried out to find the equilibrium time for optimal metal removal at 1 mg/l initial lead (II) concentration. Pseudo first order and pseudo second order kinetics were applied for modeling the biosorption process. Experiments were carried out to calculated equilibrium time. The open raceway pond was maintained at ambient temperature $(30 \pm 2^{\circ}C)$, agitator speed at 12 rpm, and pH was maintained at 7. To maintain the live culture in the biosorption medium, light intensity of 2000 lux was provided. To determine the concentration of the metal ions, the culture in the sample solutions was removed by filtration using Whatman No. 2 (8 µm) filter paper. The resulting solution was analyzed to measure the lead (II) concentration using Atomic Absorption Spectrophotometer (GBC Avanta Ver 1.32, Australia).

Pseudo first and Pseudo second order kinetics equation

Adsorption kinetics depends on process conditions, and heavy metal ions-adsorbent interactions. The kinetics should explain the mechanism and the reaction rate of adsorption system. The first adsorption kinetics of liquid-solid systems was explained by Lagergren (1898).

Legergren's first order kinetics equation

$$\log(q_{eq} - q) = \log q_{eq} - \frac{K_I}{2.303}t \qquad (1)$$

Where, q (mg/gdw) and q_{eq} (mg/gdw) is the adsorption capacity at time t (min) and at equilibrium respectively. K_1 (mg-min/gdw) is the rate constant of pseudo first order kinetics. The pseudo first order system was applied to many biosorption experiments (Kalyani et al. 2009; Cheng et al. 2015; Anirudhan and Ramachandran 2015).

The pseudo second order rate equation was applied by Ho (1995) for explaining the kinetics of adsorption of divalent metal ions onto peat. The pseudo second order rate expression which was derived based on the above mechanism (Ho 1995; Ho and Mckay 1998; Ho 2004) was given by

$$\frac{t}{q} = \frac{1}{K_{II}q_{eq}^{2}} + \frac{1}{q_{eq}}t \quad (2)$$

Where, K_{II} (gdw/mg-min) is the pseudo second order rate constant, q and q_{eq} are the adsorption capacity at time t (min) at equilibrium. A graph can be drawn between t/q and t to obtain the constants K_{II} and q_{eq} .

The present adsorption system contains adsorbent as live *Spirulina sp*, which is a blue green algae. *Spirulina* cell wall is composed of diverse array of microfibrillar polysaccharides embedded in matrix polysaccharides and proteoglycans, crystalline polymers interacting with various ions and water (Domozych 2011). The nature of the bonding between algal cell wall and metallic ions was explained by Crist et al. (1981). Due to the complex nature of the cell walls of the algal species, both covalent and ionic charge bonding may exist. The amino acids present in the proteins may provide amino, carboxy and sulfate functional groups which may be responsible for the adsorption of metal ions. These bonds are similar to the bonds that explained by Ho (1995) for peat biosorption and thus it justifies the application of the pseudo second order rate expression to the present system.

Biosorption equilibrium studies

Langmuir (1918) adsorption isotherm for physical adsorption is given by the expression

$$q_{eq} = \frac{q_{\max}bC_{eq}}{1+bC_{eq}} \quad (3)$$

Where, q_{max} (mg/gdw), indicates the monolayer adsorption capacity, 'b' (l/mg) the Langmuir constant and q_{eq} is the equilibrium adsorption capacity at metal ion equilibrium concentration C_{eq} (mg/l). The above equation can be rearranged to the following linear form:

$$\frac{C_{eq}}{q_{eq}} = \frac{1}{bq_{\max}} + \frac{1}{q_{\max}}C_{eq} \quad (4)$$

A graph between C_{eq}/q_{eq} and C_{eq} can be drawn, where b and q_{max} can be determined using slope and intercept.

An empirical relation between the concentration of the solute on the surface of an adsorbent and the concentration of the solute in the liquid was also given by Freundlich equation (1906) or Freundlich adsorption isotherm.

$$q_{eq} = K_f C_{eq}^{\ m} \tag{5}$$

Where, K_f is Freundlich constant related to adsorption capacity of adsorbent and "m" relates to the adsorption intensity. The above equation can be simplified by applying logarithm on both sides.

$$\log q_{eq} = \log K_f + m \log C_{eq}$$
 (6)

A graph can be drawn between Log q_{eq} and and Log C_{eq} and the constants K_f (mg/gdw) and 'm' can be determined using slope and intercept (Limousin et al. 2007).

Box-Behnken experimental design and artificial neural networks

Response surface methodology is an empirical modeling technique for the evaluation of the relationship of a set of controlled experimental factors and observed results. A detailed account of this technique has been outlined as performing the statistically designed experiments, estimating the coefficients in a second order polynomial mathematical model using multiple regression, predicting the responses by solving the polynomial equation and finally validating the model by performing experiments at optimal levels of the factors. A 4-factor, 3 level Box-Behnken (BB) experimental design with 3 blocks and 3 replicates at the center points, leading to 27 sets of experiments, was used for the experimental study (Siva Kiran et al. 2010; Annadurai and Sheeja 1998). The initial concentration, biosorbant dosage, agitation speed and pH were chosen as the process variables and designated as x1, x2, x3 and x4 respectively. The low, middle and high levels of each factor were designated as -1, 0 and +1 respectively (Prakash et al. 2008). The Table 2 shows the levels of process variables for all three Spirulina species. (Spirulina (Arthospira) maxima, Spirulina (Arthospira) indica, Spirulina (Arthospira) platensis). The equilibrium time at which the experiments were conducted for Spirulina (Arthospira) maxima was 7 minutes and for Spirulina (Arthospira) indica and Spirulina (Arthospira) platensis was 6 minutes from the initial studies. The experiments were conducted in open raceway pond (0.7 m long * 0.3 m wide and 0.25 m height) with working volume 25 l.

Table 2: Independent variables and their levels studied

Process Variables	Range	Leve	Levels of variables			
	studied	-1	0	+1		
x1 (Initial Concentration, mg/l)	1-10	1	5	10		
x2 (Biosorbant Dosage, gdw/l)	0.1-0.2	0.1	0.15	0.2		
x ₃ (agitation speed, rpm)	12-16	12	14	16		
x ₄ (pH)	6-8	6	7	8		

In a system involving four independent factors x_1 , x_2 , x_3 and x_4 , a mathematical equation showing the relationship of the output response factor to each and every variable can be approximated by the quadratic (second degree) polynomial equation:

$$Y = \beta_0 + \beta_1 x_1 + \beta_2 x_2 + \beta_3 x_3 + \beta_4 x_4 + \beta_{11} x_1^2 + \beta_{22} x_2^2 + \beta_{33} x_3^2 + \beta_{44} x_4^2 + \beta_{12} x_1 x_2 + \beta_{13} x_1 x_3 + \beta_{14} x_1 x_4 + \beta_{23} x_2 x_3 + \beta_{24} x_2 x_4 + \beta_{34} x_3 x_4$$

Where Y is the predicted response (% adsorption), β_0 the offset term, β_1 , β_2 , β_3 and β_4 the linear effect, β_{11} , β_{22} , β_{33} and β_{44} the squared effect, β_{12} , β_{13} , β_{14} , β_{23} , β_{24} and β_{34} the interaction effect. A multiple regression analysis is done to obtain the coefficients and the optimal values by solving four equations arising by differentiating the response variable with respect to x_1 , x_2 , x_3 and x_4 and equating them to zero. The significance of the fit explained by the polynomial models were given by the multiple coefficient of determination R². Analysis of variance (ANOVA) table was constructed to test the significance of the independent variables and their interactions (Yetilmezsoy et al. 2009). Statistica v6 (Stat Soft, USA) was used for this study.

The second order polynomial equation was further optimized for better multiple coefficient of determination and for determining the optimal values using Artificial Neural Networks (ANN) and global optimization technique. DIRECT algorithm developed by Jones et al. (1993) was implemented in Matlab Code by Tomlabs, USA (http://tomopt.com/tomlab/products/base/solvers/ glbSolve.php) was used for this study (Hu et al. 2015).

ANN is applied to complex models such as adsorption data systems (Turan et al. 2011; Yetilmezsoy and Demirel 2008; Nagata and chu 2003; Ravi et al 2009). The Levenberg–Marquardt algorithm (LMA) (More Jorge 1978) based on back propagation model, as suggested by Kaan and Sevgi (2008), was selected after comparing various algorithms present in Matlab Software for biosorption data. The equation from the artificial neural networks was loaded into the DIRECT algorithm (Chiter 2006) for calculating the optimal values. Further experiment was done to find the validity of the model at optimal conditions predicted by DIRECT global optimization technique.

Results and discussion

Toxicity of lead (II) ion on three Spirulina (Arthospira) species

Live cells of *Spirulina (Arthospira) maxima, Spirulina (Arthospira) indica, Spirulina (Arthospira) platensis* were cultivated in Zarrouk's medium with various lead (II) concentrations (0, 1, 2, 4, 10 and 20 mg/l) for finding the toxicity limits. The pH of the medium solution was found to be 9. The growth curves were shown in Figure 1.

Figure 1 shows that lead (II) concentration at 20 mg/l is highly toxic for the growth of all three *Spirulina* species. Slight decrease in *Spirulina* live cells occurred at low lead (II) concentrations below 2 mg/l. *S. (Arthrospira) indica* is more tolerant when compared with other two species *Spirulina (Arthospira) maxima* and *Spirulina (Arthospira) platensis.* The growth curves plotted for *S. (Arthrospira) indica, Spirulina (Arthospira) maxima* and *Spirulina (Arthospira) platensis* at various concentrations of zinc and nickel, by Balaji et al (2014), *S. (Arthrospira) indica* showed more tolerance, when compared with *Spirulina (Arthospira) maxima maxima* and *Spirulina (Arthospira) platensis.*

The percentage decrease in yield of *Spirulina* for all three species and the Lethal Concentration and time (LCt50) were tabulated in Table 3. The LCt50 value in mg/l was designated as 50% decrease in the productivity for 7 days. In case of *Spirulina* (*Arthospira*) platensis and *Spirulina* (*Arthospira*) indica, 50% decrease in the yield is beyond 20 mg/l lead (II) concentration at seventh day and for finding the LCt50 value, extrapolation of the data was done. The LCt50 value for *Spirulina* (*Arthospira*) maxima is in between 4 mg/l and 10 mg/l on seventh day. The



Figure 1: Growth of (a) Spirulina (Arthospira) platensis; (b) Spirulina (Arthospira) indica and (c) Spirulina (Arthospira) maxima in solutions containing aqueous lead (II) ions of various initial concentrations with light intensity of 2000 lux, a 12 h light/dark photoperiod at $30^{\circ}C\pm 2^{\circ}C$, 1: 10 inoculum ratio (0.1gdw Spirulina/), initial solution pH 9 and paddle speed 12 rpm in an open race way pond, was monitored for 8 days.

LCt50 value was found using multiple regression of the lead (II) concentrations and the percentage decrease in productivity values (Table 3: Column 1 and Column 5).

Usually, EC50 values were calculated for biological systems as reported by Chen and Pan (2005), but due to the complexity in applying various formulas and curve fitting of the data, the authors in their previous work (Siva Kiran et al. 2012) simplified the process by applying LCt50 on the *Spirulina* live cells. It is interesting to find that such type of LCt50 values were applied for the first time for *Spirulina sp.* However, the EC50 value represents only the half maximal effective concentration of lead (II) ions (plotted on x-axis) based on 50% response of the adsorption at O.D. 540 nm and it represents only the middle value present in the graph at studied concentrations of metal ions. To find the toxicity, the death of the species based on the metal ion concentrations is required. In the present work, LCt50 was used to predicts the death rate of the species at the exact metal concentration.

Biosorption of lead (II) ions in pilot scale open raceway pond

Raceway ponds are shallow ponds with depth not greater than 50 cm and varied length and breadth based on the required capacity, fitted with paddle wheels for low speed liquid mixing.

(Arthospira) platensis and Spirulina (Arthospira) indica are 95 %, 95.8% and 93.9% respectively.



Figure 2: The effect of time on lead (II) biosorption using live *Spirulina* (*Arthospira*) maxima, *Spirulina* (*Arthospira*) indica and *Spirulina* (*Arthospira*) platensis.

Table 3: Percentage decrease in the productivity and survival rate of Spirulina (Arthospira) maxima, Spirulina (Arthospira) indica, Sp	virulina
(Arthospira) platensis on exposure to various lead concentrations in pilot scale open raceway pond.	

Lead (II)	Percentage decrease in the productivity					LCt50
Concentration	Organishi	1 st day	3 rd day	7 th day	8 th day	
1		98.45	89.86	82.30	89.09	
2	Sectionality of (Arthermatica)	97.92	87.64	81.15	87.13	24.70
4	spirulina (Arinospira)	97.92	79.26	63.39	72.57	24.70 mg/1 (7 th daw)
10	platensis	92.74	74.19	57.69	60.16	(/ day)
20		92.22	73.77	52.46	59.25	
1		98.55	92.59	98.20	91.14	
2		95.65	87.65	95.90	88.45	6.4.4
4	Spirulina (Artnospira)	92.82	77.16	57.92	65.02	6.44 mg/l
10	maxima	92.10	69.13	38.49	47.65	(/ day)
20		91.37	62.96	35.54	35.33	
1		92.85	93.75	97.83	97.60	
2		88.09	89.5	95.79	97.21	42.00
4	Spirulina (Arthospira) indica	86.30	88.75	94.90	97.19	42.98 mg/l
10		88.69	76.25	66.36	67.33	(/ day)
20		87.50	77.50	61.40	62.13	

The medium components are directly exposed to the atmosphere. These types of systems are widely used in commercial scale for cultivation of algae and cyanobacteria like Spirulina sp, Chlorella sp, Anabaena sp and many others (Jorquera et al. 2010). The present study aims at using open race way pond (0.7 m long, 0.30 m wide, 0.25 m deep) for biosorption of heavy metal ions for purifying waste waters. The working volume is 25 1 and detailed conditions were given in culture conditions in materials and methods section. The effect of time on lead (II) biosorption using Spirulina (Arthospira) maxima, Spirulina (Arthospira) indica and Spirulina (Arthospira) platensis are shown in Figure 2. The organisms were added separately to open race way ponds containing 1 mg/l of lead (II) ions. The reduction in lead (II) concentration was found at regular intervals up to 1400 min (24 hrs). Maximum biosorption was observed at 7 minutes for Spirulina (Arthospira) maxima with 78.8 % of lead (II) and 6 minutes for Spirulina (Arthospira) platensis and Spirulina (Arthospira) indica with 80.6 % and 74.8 % lead (II) respectively. Further optimization of the process parameters were done at 6 minutes for Spirulina (Arthospira) platensis and Spirulina (Arthospira) indica and 7 minutes for Spirulina (Arthospira) maxima. The maximum adsorption of lead (II) ions after 24 hours for Spirulina (Arthospira) maxima, Spirulina

The adsorption rate was estimated using kinetic parameters based on lead uptake (Figure 2). This will help in selecting the optimal operation conditions for further optimization of batch process. The pseudo first order and pseudo second order equations were applied to the above system for all three species and the kinetic constants were tabulated in Table 4. For solving the first order Lagergren's equation, the equilibrium adsorption capacity qeq was assumed based on the Figure 2 and trial and error method was employed for solving the first order equation and for finding the kinetic constants. In most cases, this first order kinetics does not fit to the entire range of data and it is required to select the data points manually until the equilibrium values for better fit to the model was achieved. A graph is drawn directly for the pseudo second order kinetic equation for the entire range of data points between t/q and t. The slope and intercept were used for finding the kinetic constants (Kalyani et. al. 2009). The Figure 3 clearly states that the second order equation fits better to the above system for all three species when compared with the first order equation confirming the interaction between the functional groups on the cell wall of alga species and the heavy metal ions follows second order kinetics suggested by Ho et al. (1995).

The above results also show that very fast uptake of 74% was observed by the cells before 12 minutes at the beginning as confirmed by Chen and Pan (2005). After 12 minutes, adsorption may take place inside the cells and create gaps on the surface and

color symbols represent metal uptake or adsorption capacity q in Figure 4, the maximum metal uptake of 28.2 mg lead (II)/gdw was achieved for *S. (Arthrospira) indica*, 28.25 mg lead (II)/gdw for *S. (Arthrospira) platensis* and 27.25 mg Pb (II)/gdw for

Table 4: Kinetic constants for lead (II) ions biosorption onto live Spirulina (Arthospira) maxima, Spirulina (Arthospira) indica and Spirulina (Arthospira) platensis

Organism	Initial Conc.	Pseudo first	Pseudo first order kinetics					
Organishi	(mg/l)	k ₁	q _e	R^2	Adjusted R ²	Equation		
Spirulina (Arthospira) maxima	1	0.71807	1.9977	0.7426	0.6782	$\log(q_{eq} - q) = 0.6920 + 0.3118t$		
Spirulina (Arthospira) indica	1	1.6749	2.7926	0.9028	0.8785	$\log(q_{eq} - q) = 1.0270 + 0.7273t$		
Spirulina (Arthospira) platensis	1	1.7122	3.224	0.7784	0.7230	$\log(q_{eq} - q) = 1.1706 + 0.7435t$		
		Pseudo seco	nd order kineti	ics				
		k _{II}	q _e	R^2	Adjusted R ²	Equation		
Spirulina (Arthospira) maxima	1	0.0612	3.9326	0.9996	0.9996	t/q = 1.0567 + 0.2543t		
Spirulina (Arthospira) indica	1	0.0743	3.9793	0.9999	0.9999	t/q = 0.8499 + 0.2513t		
Spirulina (Arthospira) platensis	1	0.0591	3.8865	0.9996	0.9996	t/q = 1.1196 + 0.2573t		



Figure 3: (a) Pseudo first order and (b) Pseudo second order kinetics with regression line and multiple coefficient of regression (R²) value were shown for *Spirulina (Arthospira) maxima, Spirulina (Arthospira) indica* and *Spirulina (Arthospira) platensis*

allowing more molecules to adsorb on the surface (Swift and Forciniti 1997). The kinetic experiments studies by Chojnacka et al. (2005) for biosorption of Cr³⁺, Cd²⁺ and Cu²⁺ ion by Spirulina sp took less than 5 to 10 minutes for reaching equilibrium. Such rapid adsorption of lead metal ions by Spirulina sp is very significant as the death rate of the live Spirulina will be very less in 10 minutes. For the second order fit, the difference between adjusted R² and R² value is found to be very less and near to unity, confirming the significance of the model. For first order system, the R^2 value is far from unity and not closer to the adjusted R² showing that more number of the data points does not represent the equation or cannot be fitted into the model. Spirulina (Arthospira) indica fits well when compared with the other two species for the second order and first order system based on R^2 value. This may be due to the fact that Spirulina (Arthospira) indica has more resistance towards lead when compared with other two species based on the toxicity studies (Table 3).

The effect of initial lead (II) concentration on the biosorbent is shown in Figure 4. The experiments were performed for 7 minutes, 6 minutes and 6 minutes for *S. (Arthrospira) maxima, S. (Arthrospira) platensis* and *S. (Arthrospira) indica* respectively in open race way pond with different initial lead (II) concentrations. The percentage adsorption and *Spirulina* gram dry weigh (gdw) were measured and the adsorption capacity q (mg Lead (II)/gdw *Spirulina*) was calculated for all three species. *S. (Arthrospira) indica* showed maximum tolerance at 10 mg/l with 68.5 % lead (II) adsorption, when compared with other two species. The white

S. (Arthrospira) maxima at 10 mg/l. *S. (Arthrospira) indica* and *S. (Arthrospira) platensis* showed more tolerance for lead and can be potential adsorbent. The adsorption of the lead was not studied beyond 10 mg/l as it is suggested by Chen and Pan (2005), that at higher lead (II) concentrations, the removal rate decreased due to the saturation of active sites.



Figure 4: The effect of initial lead concentration on biosorption of *S. (Arthrospira) maxima, S. (Arthrospira) platensis and S. (Arthrospira) indica*

To find the relation between the metal uptake and equilibrium

Table 5: Langmuir and Freundlich constants and correlation coefficients for lead (II) biosorption using S. (Arthrospira) maxima, S. (Arthrospira) platensis and S. (Arthrospira) indica

Organism	Adsorption Isotherm			
S. (Arthrospira) maxima	Langmuir	b	0.2958	
	$15.4C_{m}$	q _{max}	52.08	
	$q_{eq} = \frac{eq}{1+0.2058C}$	Correlation coefficient R^2	0.9665	
	$1+0.2938C_{eq}$	Adjusted R ²	0.9582	
	Freundlich	m	0.7514	
	$q_{eq} = 11.0027 C_{eq}^{0.7514}$	$K_{ m f}$	11.0027	
		Correlation coefficient R^2	0.9984	
		Adjusted R ²	0.9979	
S. (Arthrospira) platensis	Langmuir	b	0.3137	
	$17.82C_{ac}$	q _{max}	56.81	
	$q_{eq} = \frac{eq}{1 + 0.2127C}$	Correlation coefficient R^2	0.9911	
	$1+0.513/C_{eq}$	Adjusted R ²	0.9889	
	Freundlich	m	0.7698	
	$q_{eq} = 12.5545 C_{eq}^{0.7698}$	K _f	12.5545	
		Correlation coefficient R^2	0.9819	
		Adjusted R ²	0.9774	
S. (Arthrospira) indica	Langmuir	b	0.1214	
	$12.51C_{eq}$	q _{max}	103.09	
	$q_{eq} = \frac{c_q}{1 + 0.1214C}$	Correlation coefficient R^2	0.9819	
	1+0.1214C _{eq}	Adjusted R ²	0.9774	
	Freundlich	m	0.8820	
	$q_{eq} = 10.7522C_{eq}^{0.8820}$	K _f	10.7522	
		Correlation coefficient R^2	0.9993	
		Adjusted R ²	0.9992	

concentrations, Langmuir and Freundlich models were applied for all three species (*S. (Arthrospira) maxima, S. (Arthrospira) platensis and S. (Arthrospira) indica).* The adsorption constants, coefficient of determination R^2 and adjusted R^2 along with equations were tabulated (Table 5). For all three organisms, Freundlich empirical model gave better fit when compared with the Langmuir model. There is close relation between R^2 and adjusted R^2 values for Freundlich equation, confirms the significance of the model. Our previous study on cadmium biosorption (Siva Kiran et al. 2012) with *Spirulina (Arthrospira) indica*, also fitted well with Freundlich equation, when compared with Langmuir. Similar results were also obtained by Çelekli and Bozkurt (2011) on the biosorption of nickel and cadmium on *Spirulina platensis*.

Table 6: Experimental plan of the optimization design with the experimental and predicted values for the biosorption of lead (II) ions on open raceway pond using *Spirulina (Arthospira) maxima, Spirulina (Arthospira) indica and Spirulina (Arthospira) platensis* as biosorbants.

Run No.	x ₁	x2	X3	X4	% Adsorption			A ,					
					Spirulina (Art	hospira) m	axima	Spirulina (Art	hospira) pla	atensis	Spirulina (Artho	ospira) indi	са
					Experiment	Predi	cted	Experiment	Predi	icted	Experimental	Predi	cted
					Â	BB	ANN	Â	BB	ANN	- -	BB	ANN
1	1	0.1	14	7	77.63	77.951	77.63	79.23	79.556	79.23	73.58	73.359	73.58
2	10	0.1	14	7	64.3	65.024	62.06	69.14	68.758	67.28	66.12	66.352	65.61
3	1	0.2	14	7	80.21	80.579	80.21	82.45	82.846	82.45	76.52	76.214	76.52
4	10	0.2	14	7	68.74	67.653	68.74	70.15	69.824	70.15	69.41	69.574	69.41
5	5	0.15	12	6	66.8	66.081	68.64	72.94	72.775	73.96	69.57	69.273	69.55
6	5	0.15	16	6	65.47	66.046	65.47	73.12	72.746	73.12	70.14	70.960	70.14
7	5	0.15	12	8	64.89	65.378	64.89	72.45	72.831	72.45	69.44	68.554	69.44
8	5	0.15	16	8	65.36	65.343	65.36	73.12	73.292	73.12	71.0	71.231	71
9	5	0.15	14	7	68.8	68.780	68.8	74.22	74.310	74.25	71.32	71.347	71.42
10	1	0.15	14	6	77.9	77.276	77.9	79.52	79.102	79.52	73.2	73.214	73.2
11	10	0.15	14	6	64.1	64.349	64.1	67.18	67.259	67.18	67.43	66.915	67.43
12	1	0.15	14	8	76.9	76.572	76.9	80.01	79.462	80.01	72.9	73.456	72.9
13	10	0.15	14	8	64.2	63.646	64.2	67.51	67.485	67.51	66.19	66.108	66.19
14	5	0.1	12	7	67.4	66.757	67.4	73.85	72.583	73.85	68.54	69.628	68.54
15	5	0.2	12	7	70.21	69.385	70.21	77.98	76.860	77.98	70.88	71.101	70.88
16	5	0.1	16	7	67.12	66.722	67.12	74.11	74.775	74.11	70.5	70.265	70.5
17	5	0.2	16	7	68.74	69.350	69.43	74.29	75.101	72.13	75.93	74.828	76.86
18	5	0.15	14	7	68.8	68.780	68.8	74.28	74.310	74.25	71.52	71.347	71.42
19	1	0.15	12	7	76.23	77.533	76.23	77.65	78.729	77.65	72.3	72.164	72.3
20	10	0.15	12	7	64.21	64.606	64.21	66.21	67.303	66.21	66.42	66.429	66.42
21	1	0.15	16	7	78.54	77.498	78.54	80.21	79.375	80.21	75.22	75.313	75.22
22	10	0.15	16	7	64.3	64.571	64.3	67.42	66.982	67.42	67.21	67.402	67.21
23	5	0.1	14	6	65.69	66.499	65.69	73.62	74.164	73.62	70.05	69.567	70.05
24	5	0.2	14	6	69.42	69.128	69.42	75.32	75.655	75.32	72.3	72.761	72.3
25	5	0.1	14	8	66.61	65.796	66.61	73.54	73.654	73.54	69.9	69.519	69.9
26	5	0.2	14	8	67.20	68.424	67.2	76.86	76.766	76.86	71.8	72.362	71.8
27	5	0.15	14	7	68.74	68.780	68.8	74.43	74.310	74.25	71.2	71.347	71.42

x1: Initial Concentration (mg/l); x2: Biosorbant Dosage (gdw/l); x3: Agitator Speed (rpm); x4:pH; BB: Box -Behnken;

ANN: Artificial Neural Networks

$\begin{array}{c c c c c c c c c c c c c c c c c c c $	scale open racew	ay pond		
$ \begin{array}{ll} Spirulina \\ (Arthospira) \\ maxima \\ (Arthospira) \\ maxima \\ (Arthospira) \\ platensis \\ (Arthospira) \\ platensis \\ (Arthospira) \\ indica \\ (Arthospira) \\ ndica \\ \end{array} \begin{array}{ll} Y = -65.2764 - 3.791x_1 - 104.727x_2 + 7.8x_3 + 24.138x_4 + 0.21x_1^2 + 204.66x_2^2 - 0.3096x_3^2 \\ -1.829x_4^2 + 2.266x_1x_2 - 0.054x_1x_3 + 0.064x_1x_4 - 2.975x_2x_3 - 15.7x_2x_4 + 0.225x_3x_4 \\ \hline \\ Spirulina \\ (Arthospira) \\ platensis \\ (Arthospira) \\ ndica \\ \end{array} \begin{array}{ll} Y = 9.2838 - 0.669x_1 - 43.18x_2 + 6.9430x_3 + 6.2993x_4 + 0.0132x_1^2 + 533.6667x_2^2 - 0.2036x_3^2 \\ -0.5846x_4^2 - 2.471x_1x_2 - 0.027x_1x_3 - 0.007x_1x_4 - 9.8750x_2x_3 + 8.1x_2x_4 + 0.0613x_3x_4 \\ \hline \\ Spirulina \\ (Arthospira) \\ indica \\ \hline \\ -0.873x_4^2 + 0.41x_1x_2 - 0.06x_1x_3 - 0.06x_1x_4 + 7.725x_2x_3 - 1.75x_2x_4 + 0.124x_3x_4 \\ \hline \\ \end{array} \begin{array}{ll} 0.99184 \\ 0.98232 \\ 0.98124 \\ 0.99184 \\ 0.98232 \\ \hline \\ 0.98124 \\ 0.95935 \\ 0.97063 \\ 0.93636 \\ \hline \\ 0.97063 \\ 0.93636 \\ \hline \\ \end{array}$	Organism	Second-order polynomial equation	\mathbb{R}^2	Adj. R ²
$\begin{array}{c} -1.829x_4^2 + 2.266x_1x_2 - 0.054x_1x_3 + 0.064x_1x_4 - 2.975x_2x_3 - 15.7x_2x_4 + 0.225x_3x_4 \\ \hline \\ \hline \\ maxima & & & \\ \hline \\ maxima & & \\ \hline \\ Spirulina & & \\ platensis & & \\ \hline \\ Spirulina & & \\ \hline \\ Spirulina & & \\ (Arthospira) & & \\ \hline \\ maxima & & \\ \hline \\ P = 23.492 + 0.53x_1 - 137.157x_2 + 2.107x_3 + 10.930x_4 + 231.333x_2^2 - 0.117x_3^2 \\ \hline \\ \hline \\ \\ \hline \\ \\ \hline \\ \hline \\ \hline \\ \hline \\ \hline \\ $	Spirulina (Arthospira)	$Y = -65.2764 - 3.791x_1 - 104.727x_2 + 7.8x_3 + 24.138x_4 + 0.21x_1^2 + 204.66x_2^2 - 0.3096x_3^2$	0.99184	0.98232
$ \begin{array}{ll} Spirulina \\ (Arthospira) \\ platensis \\ Spirulina \\ (Arthospira) \\ platensis \\ Indica \\ \end{array} \begin{array}{ll} Y = 9.2838 - 0.669x_1 - 43.18x_2 + 6.9430x_3 + 6.2993x_4 + 0.0132x_1^2 + 533.6667x_2^2 - 0.2036x_3^2 \\ 0.98124 \\ 0.95935 \\ 0.97063 \\ 0.93636 \\$	(Arthospira) maxima	$-1.829x_4^2 + 2.266x_1x_2 - 0.054x_1x_3 + 0.064x_1x_4 - 2.975x_2x_3 - 15.7x_2x_4 + 0.225x_3x_4$		
$\begin{array}{l} (Arthospira) \\ platensis \\ (Arthospira) \\ indica \\ \end{array} \begin{array}{l} -0.5846x_4^2 - 2.471x_1x_2 - 0.027x_1x_3 - 0.007x_1x_4 - 9.8750x_2x_3 + 8.1x_2x_4 + 0.0613x_3x_4 \\ \\ Spirulina \\ (Arthospira) \\ indica \\ \end{array} \begin{array}{l} Y = 23.492 + 0.53x_1 - 137.157x_2 + 2.107x_3 + 10.930x_4 + 231.333x_2^2 - 0.117x_3^2 \\ \\ -0.873x_4^2 + 0.41x_1x_2 - 0.06x_1x_3 - 0.06x_1x_4 + 7.725x_2x_3 - 1.75x_2x_4 + 0.124x_3x_4 \end{array} \begin{array}{l} 0.97063 \\ 0.97063 \\ 0.93636 \\ \end{array}$	Spirulina (Arthospira)	$Y = 9.2838 - 0.669x_1 - 43.18x_2 + 6.9430x_3 + 6.2993x_4 + 0.0132x_1^2 + 533.6667x_2^2 - 0.2036x_3^2$	0.98124	0.95935
$\begin{array}{l} Spirulina \\ (Arthospira) \\ indica \end{array} Y = 23.492 + 0.53x_1 - 137.157x_2 + 2.107x_3 + 10.930x_4 + 231.333x_2^2 - 0.117x_3^2 \\ -0.873x_4^2 + 0.41x_1x_2 - 0.06x_1x_3 - 0.06x_1x_4 + 7.725x_2x_3 - 1.75x_2x_4 + 0.124x_3x_4 \end{array} $ 0.97063 0.93636	platensis	$-0.5846x_4^2 - 2.471x_1x_2 - 0.027x_1x_3 - 0.007x_1x_4 - 9.8750x_2x_3 + 8.1x_2x_4 + 0.0613x_3x_4 - 0.007x_1x_4 -$		
$\begin{array}{l} (Armospira) \\ indica \\ \end{array} \qquad -0.873x_4^2 + 0.41x_1x_2 - 0.06x_1x_3 - 0.06x_1x_4 + 7.725x_2x_3 - 1.75x_2x_4 + 0.124x_3x_4 \\ \end{array}$	Spirulina (Arthospira)	$Y = 23.492 + 0.53x_1 - 137.157x_2 + 2.107x_3 + 10.930x_4 + 231.333x_2^2 - 0.117x_3^2$	0.97063	0.93636
	(Arinospira) indica	$-0.873x_4^2 + 0.41x_1x_2 - 0.06x_1x_3 - 0.06x_1x_4 + 7.725x_2x_3 - 1.75x_2x_4 + 0.124x_3x_4$		

Table 7: Second order polynomial model for the biosorption of lead onto Spirulina (Arthospira) maxima, Spirulina (Arthospira) indica and in pilot scale open raceway pond

Applications of Box-Behnken experimental design coupled with Artificial Neural Networks in biosorption of lead from three S. (Arthrospira) species.

In the preliminary step of optimization, the selected process variables were fitted to pseudo first order, pseudo second order and adsorption isotherms. The Box-Behnken experimental design is a very useful tool to determine the optimal levels and modeling of process parameters to a second order polynomial equation. The predicted response from the second order polynomial equation, the artificial neural networks and the experimental data of *S. (Arthrospira) maxima, S. (Arthrospira) platensis and*

S. (Arthrospira) indica were tabulated in Table 6. The experiments were done in open race way ponds with culture conditions given in Table 2. Each experiment was repeated three times and the average experimental results were tabulated and repeatability of the experimental results was taken care. The influence of solution pH, initial concentration of lead (II) ions, biosorbent dosage (gdw/l) and agitation speed of the paddle wheel present in the open raceway pond are studied at three levels. The regression equation obtained after application of analysis of variance was also tabulated for all three species (Table 7).

Table 8: Analysis of variance (ANOVA) for the four factorial Box Behnken Experimental design for Spirulina (Arthospira) maxima, Spirulina (Arthospira) indica and Spirulina (Arthospira) platensis

Organism	Source of	SS	DF	MS	F-Ratio	p-value
	$x_1 & x_1^2$	567.0189	2	283 5095	618 9230	0.000000
	$x_1 \ll x_1$	22 9765	2	11 4882	25 0797	0.000052
	$x_2 \& x_2$	8 2120	2	4 1060	8 9637	0.004156
	$\mathbf{x}_{1} & \mathbf{x}_{2}$	19 1418	2	9 5709	20.8940	0.000123
	ira) variation variation x1 & x12 567.0189 2 283.5095 x2 & x22 22.9765 2 111.4882 x3 & x32 8.2120 2 4.1060 x4 & x42 19.1418 2 9.5709 x1 * x2 1.0481 1 1.0481 x1 * x2 1.0481 1 0.3345 x1 * x4 0.3315 1 0.3315 x2 * x3 0.9386 1 0.9386 x1 * x4 0.3315 1 0.3315 x2 * x3 0.3540 1 0.3315 x2 * x4 2.4649 1 2.4649 x3 * x4 0.8100 1 0.8100 Error 5.4968 12 (MSE) 0.4581 Total 673.4637 26 x1 & x12 426.3905 2 213.1953 x2 & x22 23.4911 2 11.7455 x3 & x32 3.6169 2 1.8084 x4 & x42 2.0766 2 1.0383 x1 * x2 0.2358 1 0.2358 x1 * x4 0.0045 1 0.0045 x1 * x4 0.0045 1 0.0045 x1 * x4 0.6561 1 0.6661 x3 * x4 0.6561 1 0.0045 x1 * x4 0.0600 1 0.0000 Error 8.9976 12 (MSE) 0.7498 Total 479.6189 26 x1 & x12 141.2894 2 70.64471 x2 & x22 29.0380 2 14.51900 x3 & x32 13.7134 2 6.85670 x4 & x42 4.2989 2 2.14946 x1 * x3 1.1933 1 1.19326 x1 * x4 0.02771 1 0.027705 x2 * x4 0.0306 1 0.03095 x1 * x4 0.02771 1 0.227705 x2 * x4 0.0306 1 0.03003 x2 * x4 0.0306 1 0.03003 x2 * x4 0.02450 1 0.024503 Error 5.9279 12 (MSE) 0.49399 Total 201.8117 26 Hore	2 2880	0.156256			
Spiruling (Arthospira)	X1* X2	0.9386	1	0.9386	2.2880	0.177834
marima	X1+X3	0.3315	1	0.3315	0.7237	0.411571
maxima	A]* A4	0.3513	1	0.3540	0.7237	0.306506
	A2* A3	2 4640	1	2 4649	5 2811	0.0390390
	A2* A4	0.8100	1	0.8100	1 7692	0.008787
	X3* X4	5 4068	1	(MSE) 0.4591	1.7085	0.206517
	Total	5.4908	26	(MSE) 0.4381		
	10tai	426 2005	20	212 1052	204 2254	0.00000
	$X_1 \propto X_1$	420.3903	2	213.1933	284.3334	0.000000
	$\frac{X_2 \alpha X_2}{\alpha \alpha x_2}$	23.4911	2	11./455	2 4110	0.000431
Spirulina (Arthospira) maxima Spirulina (Arthospira) platensis Spirulina (Arthospira) indica	$X_3 \propto X_3$	3.0109	2	1.8084	2.4119	0.131089
	$x_4 \propto x_4$	2.0700	2	1.0383	1.3848	0.28/038
	X ₁ * X ₂	1.2466	1	1.2466	1.0020	0.221550
Spirulina (Arthospira)	X ₁ * X ₃	0.2358	1	0.2358	0.3145	0.585257
platensis	X ₁ * X ₄	0.0045	1	0.0045	0.0060	0.939316
	X2* X3	3.9006	1	3.9006	5.2022	0.041615
	x _{2*} x ₄	0.6561	1	0.6561	0.8750	0.368010
	X3* X4	0.0600	1	0.0600	0.0801	0.782045
	Error	8.99/6	12	(MSE) 0.7498		
	Total	4/9.6189	26			
	$x_1 \& x_1^2$	141.2894	2	70.64471	143.0075	0.000000
	$x_2 \& x_2^2$	29.0380	2	14.51900	29.3911	0.000024
	$x_3 \& x_3^2$	13.7134	2	6.85670	13.8802	0.000756
	$x_4 \& x_4^2$	4.2989	SS DF MS F-Ratio 567.0189 2 283.5095 618.9230 22.9765 2 11.4882 25.0797 8.2120 2 4.1060 8.9637 19.1418 2 9.5709 20.8940 1.0481 1 0.9386 2.0490 0.3315 1 0.3315 0.7237 0.3540 1 0.3540 0.7729 2.4649 1 2.4649 5.3811 0.8100 1 0.8100 1.7683 5.4968 12 (MSE) 0.4581 673.4637 673.4637 26 - 426.3905 2 213.1953 284.3354 23.4911 2 11.7455 15.6648 3.6169 2 1.8084 2.4119 2.0766 2 1.0383 1.3848 1.2466 1.6626 0.2358 1 0.2358 0.3145 0.0060 3.9006 1 3.9006 5.2022 0.6561 0.8750<	0.037928		
	x _{1*} x ₂	0.0339	1	0.03395	0.0687	0.797660
Spirulina (Arthospira)	X1* X3	1.1933	1	1.19326	2.4155	0.146102
indica	$x_1 * x_4$	0.2771	1	0.27705	0.5608	0.468348
	X2* X3	2.3870	1	2.38703	4.8321	0.048292
	x _{2*} x ₄	0.0306	1	0.03063	0.0620	0.807581
	x _{3*} x ₄	0.2450	1	0.24503	0.4960	0.494700
	Error	5.9279	12	(MSE) 0.49399		
	Total	201.8117	26			

DF: Degree of freedom; SS: Sum of squares; MS: mean squares (SS/DF); MSE: Mean Square Error; F: F-Statistics (MS/MSE), p-value: The probability of the actual event observed, together with any other equally extreme or more extreme events that might have occurred and for the above experimental data, p-value was calculated by Statistica v7.0 (Statsoft, USA).

By applying the multiple regression analysis on the above factors and the final adsorption values of all three species, given in Table 6, the following second order polynomial equations were found (Table 7).

Where Y is the predicted lead (II) adsorption percentage and x_1 , x_2 , x_3 and x_4 are the coded terms for initial concentration (mg/l), biosorbant dosage (gdw/l), agitator speed (rpm) and pH respectively. The difference between R² and adjusted R², was also tabulated for the above equations for better understanding of the above data. The value of the coefficient of determination (R² = 0.99184) for *Spirulina (Arthospira) maxima* indicates that only 0.816 (1- R²) percentage of the total variations in the independent variables (x₁, x₂, x₃ and x₄) were not explained by the model equation. The adjusted R² values explain the descriptive power of regression model equations. Every data

point added to the model increases the R^2 value for better fit but adjusted R^2 compensates for the addition of variable and it increases and becomes close to the R^2 only if the experimental data points enhances the model and decreases when the data points enhances the model less. Liu et al. (2004) explained about the adjusted R^2 , that it corrects the R^2 value for the entire sample size and the number of terms in the model. If there are many terms in the model which does not fits to the equation and the sample size is not very large, adjusted R^2 may be noticeably smaller than the R^2 . The value of the adjusted coefficient of determination (Adj $R^2 = 0.98232$) for *Spirulina (Arthospira) maxima*, are near to the R^2 confirming that that many terms in the model fits the equation.

It is clear from the above values, that the R² is greater than 0.95 for all three equations showing that the experimental data fits to speed (rpm) pH Desirability



Figure 5: Profiles for predicted values and desirability showing the individual parametric effects on the adsorption of lead (II) ions on a) Spirulina (Arthospira) maxima, b) Spirulina (Arthospira) indica and c) Spirulina (Arthospira) platensis.

the predicted equation and the adjusted R^2 value is near to the R^2 for *Spirulina (Arthospira) maxima* and lot of variation was found for other two species. This signifies that most of the experimental data points were fitted significantly to the predicted equation for *Spirulina (Arthospira) maxima* when compared with *Spirulina (Arthospira) platensis* and *Spirulina (Arthospira) indica*. Thus requires better models for fitting the complex experimental data to include those left over data points for better fitness and for better predictability of the second order polynomial equations. The optimal values were obtained by differentiating the above three equations with respect to x_1 , x_2 , x_3 and x_4 and solving the four equations by equating them to zero. The equations were also analyzed by plotting response surface contour plots and calculating ANOVA (Analysis of Variance - Table 8).

The significance of independent variables and their interactions with each other during the experimentations and for in-depth analysis to find out the most significant process variable which influences the yield were found by ANOVA (Table 8) (Yetilmezsoy et. al. 2009). The p-values and F-values are used as tools to check the significance of each independent variable and also indicates the interaction between them. The smaller the pvalue and higher the F-ratio, the more significant the independent variable will become. In the above ANOVA table, initial concentration (mg/l) is found to be more significant when compared with other three independent variables for all three species and next significant factor was found to be live Spirulina adsorbant dosage. Agitation speed was found to be more significant for Spirulina (Arthospira) platensis and Spirulina (Arthospira) indica, when compared to pH. This shows that the selected range of pH is very low (6-8) to show the actual effect on these two species as the solution pH is one of the most important factors of biosorption process, drastically affecting the surface charges on the cell walls of *Spriulina*. Mitrogiannis et al. (2015), showed that biomass of *S* (*Arthospira*) platensis has optimal initial pH of 7.5 with suitable pH range of 6 to 8. For better understanding of the ANOVA table for the *Spirulina* (*Arthospira*) maxima, *Spirulina* (*Arthospira*) indica and *Spirulina* (*Arthospira*) platensis, profiles for predicted values and desirability graphs were plotted (Figure 5) using Statistica V7.0 (Statsoft, USA).

A prediction profile for the initial concentration (mg/l), biosorbant dosage (gdw/l), agitator speed (rpm) and pH for lead (II) ions biosorption on *Spirulina (Arthospira) maxima, Spirulina (Arthospira) indica* and *Spirulina (Arthospira) platensis* consists of series of graphs of predicted percentage adsorption values for each independent variable and holding the levels of the other independent variables constant. Each individual graph shows the pattern of variation of the percentage adsorption of lead at different levels. Using the above graphs, better understanding of the predicted responses and the most desirable response on the dependent variable can be found (Statistica V7.0, Stafsoft, USA).

If we closely observe the values of initial concentration studied for the Box-Behnken experimental design, (1, 5 and 10 mg/l), the toxicity increases as the metal concentration increases and at high toxicity, the *Spirulina sp.* tends to die leading to the less number of *Spirulina* cells available for biosorption of lead., At low initial concentrations the adsorption percentage will be high and the same pattern was also shown in Figure 4. Chen and Pan (2005), also showed that, as the initial concentration of lead (II) ions increases, the percentage adsorption tends to decreased due to the toxicity and the saturation of the adsorption sites above 20 mg/l. Increase in biosorbent dosage, the percentage adsorption tends to increase and the above graphs clearly shows that when more *Spirulina* was added and more adsorption sites will be available



Figure 6: Response surface contour plots for continuous monitoring of the initial concentration (mg/l), biosorbant dosage (gdw/l), agitator speed (rpm) and pH for lead (II) ions biosorption on *Spirulina (Arthospira) maxima*

0.22

904

and more biosorption may take place and the pattern was found to be same for all three *Spirulina sp.* The agitation speed and pH first increased and afterwards decreased for all three species, showing the possibility of getting optimal agitation speed and pH values. Probably at high agitation speeds, more rupture and cell breakage of *Spirulina* might take place leading to the death of many *Spirulina* cells and at low agitation speed, enough contact between the cell walls and the lead (II) ions may be present. Olguin (1994), studied on growth of *Spirulina sp.* at different agitation speeds and found that the variation in growth is unbalanced and not following any pattern. Optimal pH was found to be about 7 and it has to be further verified by solving the above predicted equations tabulated in Table 7. The two dimensional contour plots were drawn to determine the interactions of the initial concentration, biosorbant dosage, agitator speed and pH on adsorption of lead (II) ions on to *Spirulina (Arthospira) maxima, Spirulina (Arthospira) indica* and *Spirulina (Arthospira) platensis*. The Figures 6, Figure 7 and Figure 8, shows the relative interaction of any two factors when the other two factors were maintained at constant level. In Figure 6, pH and agitation speed showed correct pattern by giving optimal values at pH 7 and agitation speed 14 rpm, the remaining graphs are considered to be having saddle points i.e. they are having curves up in one direction and curves down in other direction and does not have optimal points. The circle represents optima minima or optima maxima and the trend towards reaching



Figure 7: Response surface contour plots for continuous monitoring of the initial concentration (mg/l), biosorbant dosage (gdw/l), agitator Speed (rpm) and pH for lead (II) ions biosorption on Spirulina (Arthospira) indica

Derringer and Suich (1980) developed a procedure for specifying the relationship between predicted responses (percentage biosorption) on a dependent variable and the desirability of the responses which is called as the desirability function. He also formulated a procedure that provides three "inflection" points in the function represented in the graph. The score "0" can tend to be less desirable and score "1" is highly desirable and score "0.5" can be in between factor. The "higher is better", desirability function was used for plotting the above graph. As the graph clearly shows that at lowest initial concentrations, the highest desirability score was shown for all three species. The average range is found to be from 60 % to 83 % for all experiments (desirability values) shown in Figure 5. Response surface contour plots were plotted for finding the optimal values and understanding the interactive responses between each factor (Figure 6, Figure 7 and Figure 8).

the circle, represents that the system is reaching towards the optimal adsorption rate. Here in the above graphs, optima maxima was achieved. The graphs, between pH and biosorbant dosage and agitation speed and biosorbant dosage, the optimal pH is approximately near to 6.6 and 7.4 and optimal agitation speed is at approximately between 13.5 rpm and 14.5 rpm but the both graph tends to move towards highest biosorbent dosage. At 0.12 gdw/l biosorbent dosage the percentage removal of lead (II) ions is low and at 0.22 gdw/l, the biosorbent dosage is high and the graph trend is moving towards higher biosorbent dosage for higher percentage adsorption. These graphs will help in in-depth analysis of the variation of the independent variables.

Figure 7 shows maximum biosorption was found to be near pH 6.8 and 7.4 and agitation speed beyond 16 rpm. The remaining graphs found to be more saddle points with curve patterns at

different directions leading to no specific conclusion. But graphs including initial concentration shows that at low initial concentrations, the percentage adsorption is high and at high biosorbent dosage i.e. >22 gdw/l, the adsorption percentage is found to be high. The graph trend seems to be complicated and may affect the prediction of optimal points.

like training function, transfer function, error, training set selection or construction of topology for the neural networks. The choice of the design parameters for the neural networks was determined by trial and error method. In present study, the testing experimental run data set and along with other parameters were



Figure 8: Response surface contour plots for continuous monitoring of the initial concentration (mg/l), biosorbant dosage (gdw/l), agitator Speed (rpm) and pH for lead (II) ions biosorption on *Spirulina (Arthospira) platensis*

For Spirulina (Arthospira) platensis the optimal pH, lies in the range of 7.0 to 7.4 and optimal agitation speed (rpm) in the range of 13.5 rpm to 14.5 rpm and is approximately similar to the other two species. The other graphs showed saddle points with one or more optimal points but following the same pattern that at low concentrations the yield is high and at high biosorbent dosage the removal rate is less. Table 10 showed predicted responses at optimal Initial concentration, biosorbant dosage, agitator speed and pH of the all three species. The values from the Box-Benkehn results failed to predict the exact parameters. Some initial concentration values were shown negative and some beyond 500 mg/l which were absolutely wrong and the predicted percentage also goes beyond 100 %. The same saddle pattern was also shown in the above contour graphs and still more advanced stochastic models are required to predict the optimal points from the Box-Behnken Experimental design data.

The input and hidden layers included for the above experimental data and network topology used are given in Table 9 along with the back propagation training function. For testing, the run numbers, 2, 5, 17 and 27 were used for all three species and the remaining experimental runs were used for training. As per Nagata and Chu (2003), there are no specific guidelines exist for the selection of any of the above mentioned design parameters

selected after running various trials and comparing the results for better Coefficient of Determination (R^2) value.

The configuration of the neural network developed in this work (Eg: 4-24-1 structure: four input neurons - twenty four neurons in hidden layer - one output neuron - *Spirulina (Arthospira) maxima* - Table 9 - Column 2) was determined by trial and error method. Because of the empirical nature of the neural networks, the data sometimes will not extrapolate well and final experimentation is also required to prove the validity of the predicted model.

Ravi et al (2012), suggested an equation for neural network training for calculation of weights and bias by the artificial neural networks. A non linear mapping between the input parameters, for the experimental runs was determined based on the equation suggested by Ravi et. al. (2012). The equation contains the input parameters $(x_1, x_2, x_3 \text{ and } x_4)$, output parameters (y) and weights and the bias suggested by the neural networks based on the training using training function "trainlm".

$$y = w_2 * \left(\frac{2}{1.0 + e^{-2/(w_1 * x v^1 + b_1)}} - 1\right) + b_2$$

Where w_1 and w_2 are the weights, b_1 and b_2 are the biases (Table 9). 'y' is the predicted value from the neural network and

functions available in Matlab Software (trainbr, trainb etc..), number of iterations were changed until maximum R^2 was

Table 9: Weights and biases of the neural networks for modeling the Box-Behnken experimental design data for biosorption of lead (II) ions on live Spirulina (Arthospira) maxima, Spirulina (Arthospira) indica and Spirulina (Arthospira) platensis in open race way pond

Organism	Training	Weights and	biases of the neu	ral networks	· ·	51		
C	function	wl				w2	b1	b2
		-0.4023	-0.8513	-0.9613	-0.5166	-8.49949	-6.0254	19.3431
		-4.4069	-0.9581	3.9656	-0.6618	1.355852	-1.3374	
		3.0092	-1.1843	1.9048	-2.2567	-1.05383	1.3157	
		2.1115	0.7533	-0.5915	1.4802	4.36521	7.9427	
Organism Spirulina (Arthospira) maxima Spirulina (Arthospira) platensis		1.3216	0.1163	-0.7143	-1.427	-4.56108	-7.8747	
		0.9834	0.83	-0.8622	-1.3878	3.091108	6.2305	
		0.6892	-1 1841	0.2713	-0.2223	-1.02376	-4 3593	
		-0.2066	-3 2524	0.0686	-0.5282	1 513502	-6.0771	
		2 1369	-2 296	0.3598	2 5792	-3.06022	-0.6159	
	Levenberg	5 709	1 9422	-0 4444	0.5041	1 642421	-2.705	
	-Marquadt	4 8720	0.8126	0.0253	0.7382	2 02/2	1 5747	
Spirulina	(trainlm)	2 6285	1.0821	4 2260	-0.7382	0.504238	0.0460	
(Arthospira)		1 7605	2 4045	3.0008	2 6427	0.394338	-0.0409	-
maxima	$R^2 = 0.99365$	0.077	0.1044	0.6916	-2.0437	2 12004	2 4064	-
	24 Neurons	2 1542	-0.1044	-0.0810	2.0667	-3.12004	-3.4004	-
	(4-24-1)	1.0004	0.0372	1 2220	1.2500	-2.11461	-0.298	
		-1.0004	-2.2383	-1.2329	-1.3399	0.62507	2.5750	
		-0.4481	-1.9352	-2.9831	-0.34/9	-0.03397	-2.3739	
		0.1899	1.3917	-1.//04	2.4433	4.969359	3.9644	
		0.1297	1.0227	-0.2433	-0.9508	0.114859	4.8/13	
		-2.4154	1./099	0.4518	-1.0939	1.902598	6.3779	
		-4.9597	2.3579	-1.5192	4.6358	3.65//21	/.9318	
		1.7476	1.3149	2.4148	2.4294	-6./1012	-6.80/3	
		-8.1011	1.8651	-2.9016	-2.1645	-1.3302	2.6285	
		-0.6502	0.0804	1.111	-1.1358	9.850148	5.1247	
		-0.0155	-1.4025	0.4956	1.1872	-13.5375	-3.7446	32.3216
		3.0142	-8.4843	5.1057	5.8793	3.0359	-3.3421	
	Tarrahan	-0.6657	-0.3903	-0.9053	0.7541	5.639	3.7168	
		-2.5438	6.6103	7.3067	-6.8031	2.0296	6.8958	
		1.4274	0.4812	1.8743	1.0842	-7.5783	-2.5739	
	Levenberg	-0.2137	-1.4548	-0.0954	0.6175	2.7795	3.8837	
Spiruling	-ivial quadi	0.2724	-4.1507	-4.9706	4.5502	-2.4707	-1.5138	
(Arthospira)	(uaiiiiii)	1.7752	1.063	-0.5782	-2.0862	-4.8859	-4.529	
(Arthospira)	$R^2 = 0.99133$	-0.8381	3.4265	1.2659	0.6536	0.7303	0.7223	
pratensis	16 Neurons	-3.7264	-0.9188	-1.8383	0.5934	2.7487	-2.0942	
	(4-16-1)	6.8246	0.881	5.4059	3.2231	-3.3854	-2.6885	
	(. 10 1)	2.7314	-3.144	-0.1441	-2.0888	-1.8834	1.5049	
		-3.6704	0.932	-2.2885	0.3539	2.5188	8.1595	
		-5.7881	-4.1583	-2.9772	-2.875	-2.9315	3.0827	
		0.7246	-0.1939	0.5853	-1.4286	-9.323	-4.4534	
		7.6032	-9.5617	-0.0415	7.7447	2.3029	-8.4334	
		-1.2104	-1.6347	-1.9083	2.7642	9.6041	2.5878	36.6874
		-7.6862	-2.8572	-2.7228	5.297	1.704	-3.978	
		-1.6642	-0.0331	5.5177	-0.6777	9.0509	11.8496	
		-0.6631	4.0782	0.2409	-0.1494	4.1176	9.6424	
		-0.918	1.2658	0.5173	1.0422	1.0796	4.2038	
	Levenberg	0.854	-0.7178	0.0142	-1.9428	0.0631	-1.0814	
	-Marquadt	0.1877	-4.2794	-1.7238	1.053	-1.0696	2.1991	
a · 1·	(trainlm)	0.0992	-0.9447	-1.3344	4.1519	-0.5563	0.5698	
Spirulina	Ì`´´	-2.7054	-0.5269	0.631	-0.0293	3.3779	1.5036	
(Arthospira) indica	$R^2 = 0.9979$	-1.7581	-2.5563	-6.2118	-2.2055	-2.4377	-6.0178	
	17 Neurons	1.7577	1.5734	0.3791	2.3608	-2.6487	-2.851	
	(4-17-1)	-1.0622	5.1582	2.3588	2.6083	-1.6445	0.5761	
		-2.5824	-0.5376	0.1074	-6.2088	1.7371	3.8388	İ
		-1.8462	5.1077	-0.7472	0.0858	2.0359	1.1326	1
Spirulina (Arthospira) platensis Spirulina (Arthospira) indica		-1.4301	-0.6751	-0.0834	-2.3528	5.1295	3.506	1
		-3.9038	-2.9297	-0.6901	0.7272	7.8448	9.0402	1
		-9.5101	-6.27	-5.9499	0.5251	-9.7264	4.7664	1
	1							

xv is the row vector of 4 independent variables $(x_1, x_2, x_3 \text{ and } x_4)$, while **xv**¹ represent the transpose of the vector with a dimension of (4x1). A matlab code was written using "postreg" function to test the training data with testing data and for finding the coefficient of regression (R²). , the parameters like total number of neurons, testing set, mean square error, various training

achieved. After considerable number of trials, the testing set, training set, training function was finalized and the optimal numbers of hidden neurons were found. The theoretical and calculated weights and bias for all three species was optimized using DIRECT algorithm suggested by Jones et al. (1993).

The optimal values predicted by Box-Behnken experimental design by solving four equations arising by differentiating the response variable of the equations given in Table 7 for all three Table 10: Optimized values predicted by global optimization algorithm linked to artificial neural networks

lead (II) concentration and high for biosorbent dosage. Our interest is to find the optimal maximum lead (II) removal within the confined region of experimentation levels. The DIRECT

Organism Name	Optimized values based on the model equation								
		Initial	Biosorbant	Biosorbant	pН	% A	dsorption		
		Concentration (mg/l)	Dosage (gdw/l)	Dosage (gdw/l)		Predicted	Experimental		
Spirulina	Box-Benkhen	88.96652	0.08579	13.98587	6.90389	64.74	-		
(Arthospira) maxima	Experimental Design								
Spirulina	Box-Benkhen	557.5316	0.1288	14.1217	7.176	40.167	-		
(Arthospira) platensis	Experimental Design								
Spirulina	Box-Benkhen	-387.475	0.085	16.282	6.930	87.3617	-		
(Arthospira) indica	Experimental Design								
Spirulina	Artificial Neural	10.1852	0.164815	13.9342	7.14815	80.7175	79.32		
(Arthospira) maxima	Networks								
Spirulina	Artificial Neural	10.0617	0.138477	15.284	7.53498	88.1518	83.58		
(Arthospira) platensis	Networks								
Spirulina	Artificial Neural	48.3333	0.177984	15.6461	7.37037	90.2168	91.15		
(Arthospira) indica	Networks								

species and artificial neural networks using DIRECT algorithm were tabulated in Table 10. The initial concentration for *Spirulina (Arthospira) platensis* and negative concentration for *Spirulina (Arthospira) indica* are not acceptable. The fact that Box-Behnken failed to predict lies in the profile prediction graphs of

algorithm coupled with artificial neural intelligence had successfully predicted the values and the predicted response is high when compared with any value in the experimental result (Table 6) for all three species. This demonstrates the superiority of the ANN and the DIRECT algorithm when compared with



Figure 9: The three graphs shows, the predicted percentage adsorption from second order polynomial equation from Box-Behnken experimental design, equation from weights and bias from artificial neural networks, and the regression line with the experimental percentage adsorption for *a*) *Spirulina (Arthospira) maxima, b*) *Spirulina (Arthospira) indica* and c) *Spirulina (Arthospira) platensis.*

initial lead (II) concentration and biosorbent dosage is shown in the Figure 5. When concentration decreases, the adsorption increases and when biosorbant dosage increases, then adsorption percentage increases. If the data is blindly extrapolated or interpolated without applying non linear stochastic intelligent algorithms, the predicted values will become negative for initial Box-Behnken experimental design. The Box-Behnken predicted values were neglected as it is impossible to maintain negative predicted concentrations and near zero biosorbant dosage. The neural network model not only fits the training data very well but also provides predictions of the validation data very close to those measured experimentally (Nagata and Chu 2003). The open circles in the above diagram (Figure 9), which are little far to the regression line are the predicted responses from the ANN and are excluded from the actual training.

Conclusions

In this present work, the importance of using live Spirulina sp. for biosorption of heavy metal ions and the importance and possibility of using algal open raceway ponds for waste water treatment was explored. The growth and toxicity studies of live cells of S. (Arthrospira) maxima, S. (Arthrospira) indica and S. (Arthrospira) platensis in algal open raceway ponds were done. Spirulina (Arthrospira) indica is more tolerant when compared with other two species. The LCt50 values for all three species were estimated. The same algal open raceway pond were used for biosorption of lead using live Spirulina sp. and models like, Lagergren's first order equation, pseudo second order equation and Langmuir and Freundlich adsorption isotherms were fitted to the adsorption experimental data. Empirical model building like second order polynomial equation was a standard approach for handling statistical experimental designs like Box-Behnken was used for the present study, it is found that neural networks provided better fit when compared with conventional quadratic model. The DIRECT algorithm is successfully applied for the first time in finding the optimal values for complex biosorption systems using Spirulina sp. This study establishes the possibility of using open race way ponds for wastewater treatments and superiority of using ANN systems coupled with DIRECT algorithm for handling complex adsorption multi-factorial systems.

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